

Algebra 2

3.3 Complex Number Operations

Complex #'s : $a + bi$

i is called the imaginary unit

$$\sqrt{i^2} = \sqrt{-1} \quad i = \sqrt{-1}$$

Square Roots of Negative Numbers

$$1) \sqrt{-5} = \sqrt{-1 \cdot 5} = \sqrt{-1} \sqrt{5} = \boxed{i\sqrt{5}}$$

$$2) \sqrt{-6} = i\sqrt{6}$$

$$3) \sqrt{-100} = 10i$$

Multiplying Pure Imaginary Numbers

Remember $i^2 = -1$

Simplify

$$1) -2i \cdot 7i = -14i^2 = -14(-1) = \boxed{14}$$

$$2) -6i \cdot -4i = 24i^2 = 24(-1) = \boxed{-24}$$

$$\begin{aligned} 3) -3i \cdot -2i \cdot 7i &= 42i^3 = 42i^2 \cdot i \\ &= 42(-1) \cdot i \\ &= \boxed{-42i} \end{aligned}$$

Simplifying a Power of i remember $i^2 = -1$

Simplify i^{45}

$$i \cdot i^{44}$$

$$i \cdot (i^2)^{22}$$

$$i \cdot (-1)^{22}$$

$$i \cdot 1$$

$$\boxed{i}$$

Simplify i^{35}

$$i \cdot i^{34}$$

$$i \cdot (i^2)^{17}$$

$$i \cdot (-1)^{17}$$

$$i \cdot -1$$

$$\boxed{-i}$$

Adding/Subtracting Complex Numbers

$$1. 7i + 9i = \boxed{16i}$$

$$2. \underbrace{(-5 + 6i)} + \underbrace{(2 - 11i)}$$
$$\boxed{-3 - 5i}$$

$$3. (2 + 3i) - 1(4 + 2i)$$
$$\underbrace{2 + 3i} - \underbrace{4 - 2i}$$
$$\boxed{-2 + i}$$

Try this: Simplify

$$1) i^{\frac{144}{2}} = (i^2)^{\boxed{72}}$$
$$(-1)^{\boxed{72}}$$
$$\boxed{1}$$

$$2) (4+3i) - (-2+7i)$$

$$4+3i+2-7i$$

$$\boxed{6-4i}$$

$$3) -4i \cdot 7i$$
$$-28i^2 = -28(-1)$$
$$= \boxed{28}$$

$$4) i\sqrt{-25}$$
$$\boxed{5i}$$

Algebra 2
Imaginary Numbers WS

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Simplify

1) $\sqrt{-36}$

2) $(6i)(-2i)$

3) i^{29}

4) i^{38}

5) $(2 - 8i) - 4i$

$$6) \sqrt{-3}$$

$$7) -2i \cdot -6i \cdot 4i$$

$$8) -7i + 10i$$

$$9) 3i - (5 - 2i)$$

$$10) (-2 + 8i) - (7 + 3i)$$